MEASUREMENTS OF THE VERTICAL DISTRIBUTION OF THE VOID FRACTION USING X-RAY ATTENUATION FOR DIFFERENT FLOW REGIMES IN A HORIZONTAL PIPE

L. Rossi, R. de Fayard, S. Kassab CEA, CEA Saclay, DEN, DANS/DM2S/STMF/LIEFT 91191 Gif-sur-Yvette, France lionel.rossi@cea.fr; rossi_lionel@yahoo.fr

ABSTRACT

METERO is an experimental facility built by the French Atomic Energy Commission (CEA) aimed at studying adiabatic air-water flows in horizontal pipes. The physical insight and the experimental data provided by METERO experiments support the validation of MCFD and CATHARE-3 codes as part of the NEPTUNE project developed jointly by EDF, CEA, AREVA NP and IRSN. Botin et al. Int. J. Multiph. Flow 2014 have proposed a flow map of the different regimes encountered in the METERO experiments, i.e. stratified flows, slug flows, plug flows, stratified dispersed bubbly flows and dispersed bubbly flows. Following this work, we investigate the vertical distribution of the void fraction integrated horizontally using X-ray attenuation measurements.

The X-ray attenuation provides integrative measurements along the X-ray path. To obtain the vertical distribution of the void fraction integrated in the horizontal direction, the X-ray apparatus is rotated to ensure a spatial resolution of about 1mm. For METERO's pipe of 100mm diameter, this provides a fine discretisation of the void fraction distribution with a reasonable amount of realisations, i.e. 7 angles.1

After a brief description of the experiments and the measurements' method, we discuss the evolution of the vertical distribution of the void fraction in horizontal pipes. Different flow regimes and their transitions (e.g. slug, plug, and bubbly regimes) are explored by varying the water and air superficial velocities.

In addition to the quantification of the vertical distribution of void fraction, these X-ray measurements support the highlighting of non-linear processes related to the establishment of void fraction profiles. Moreover, the quantification of the void fraction over the flow cross-section, αS , and the ratio of air and water phase velocities are discussed. For slug flows (at 41.3D) the trends $\alpha_S \sim \frac{3}{5} \alpha_Q$ and $\frac{U_{air}}{U_{wat}} \sim \frac{5}{3} \alpha_Q$, where αQ is the void fraction where the air is injected, are observed in the present experiments.

KEYWORDS Flow regime, X-ray measurements, void fraction, horizontal pipe

¹ It can be noted that to obtain similar results with optical probe measurements, at least 100 acquisitions would be needed for each profile. Moreover, for optical probes measurements, hypotheses about the data integration need to be done so as to extract the integral along the horizontal direction and/or the number of acquisitions needs to be increased well above 100. X-ray attenuation measurements are then an interesting tool to investigate the vertical distribution of the void fraction over a broad range of flow conditions.

1. INTRODUCTION

Vertical bubbly flows have been extensively studied, e.g. [1,2,3,4,5] whilst less literature can be found about multiphase flows in horizontal pipes, e.g. [6,7,8]. The dynamic of multiphase flows in horizontal pipes differs from the one observed in vertical pipes due to the fact that gravity is perpendicular to the mean flow and not parallel. The buoyancy forces tend to have bubbles moving up. They then support the accumulation of air in the upper part of the pipe which favours the coalescence of bubbles. The turbulence is amenable to disperse bubbles and to provoke the coalescence and break up of bubbles. The competition between buoyancy and turbulent forces in horizontal pipes results in different flow regimes from stratified flows to dispersed bubbly flows [8].

The pipes' lengths of nuclear power plant are generally (primary circuit) about ten times their diameters. Potential multiphase flows in such short pipes would not reach a fully developed stage. The knowledge, modelling and simulation of transient horizontal two-phase flows are therefore important for safety studies of nuclear power plant. Existing literature and experimental data need to be completed by experiments in relatively short pipes.

METERO is an experimental facility built by the French Atomic Energy Commission (CEA) aimed at studying adiabatic air-water flows in horizontal pipes. The physical insight and the experimental data provided by METERO experiments support the validation of MCFD and CATHARE-3 codes as a part of the NEPTUNE project developed jointly by EDF, CEA, AREVA NP and IRSN. The main purpose of METERO experiments is to help improving the accuracy of numerical tools by providing new physical insights and data for validation.

Measurements using X-ray attenuation are amenable to indicate the structures of multiphase flows where the phases' attenuations are different, e.g. [9,10,11,12,13]. The void fraction within air-water flows can then be measured using X-ray attenuation. Using such measurements, the present manuscript focuses on the vertical distribution of the void fraction and deduces physical quantities such as air and water phase velocities.

The manuscript is articulated as follows. First the experimental rig, the measurement methods and the flows' parameters investigated are introduced. Then results obtained from measurements performed over different flow regimes and at different longitudinal positions (10.4D, 20.6D and 41.3D) are presented and discussed.

2. Experimental description

2.1. Experimental setup

METERO is an experimental rig dedicated to the study of turbulent mixing of air and water in horizontal flows. Extensive descriptions of METERO can be found in [14,15,8].

The pipe is of circular shape and is assembled from different modules made in Perspex. The Perspex walls are 10mm thick. The inside diameter of the pipe, i.e. the diameter of the flow cross section, is D=100mm. D is chosen as the reference length scale. Dimensionless length scales, according to D, are noted with a superscript star, e.g. $y^* = y/D$. Fig. 1a is a photo of METERO's test section.

The water flow rate within the pipe section is noted Q_{wat} . It is measured using either MHD (electromagnetic) or Coriolis flow meters according to the flow intensity. At the entrance of the test section, the air is regularly injected in space over 37 nozzles with inside diameters of 1.2mm. The air flow rate is measured using mass flow meters and is noted Q_{air} . 3.76D downstream the injection, a turbulent grid (mesh of 2.71mm with wires of 0.71mm diameter) mixes the flow and breaks air bubbles. The longitudinal (or flow) direction along the pipe is noted x and the vertical direction is noted y. The position of the grid is chosen as the x axis origin. The axis of the pipe is chosen as the origin of y. Fig. 1b illustrates these positions and notations. Downstream the test section, a water tank at atmospheric pressure is used to separate the air from the water. This black tank is visible on the right of figure Fig. 1a.



Figure 1: (a) photo of the test section with the encapsulated X-ray source and of the X-ray detector mounted on a rotating device; (b) schematic of the test section with relevant longitudinal positions; (c) schema of the X-ray source and the angular distribution of X-ray beams crossing the test section.

The X-ray beams are emitted from a localised source at 160kV and 18.75mA. It is collimated so as to illuminate a plane perpendicular to the axis of the test section. Fig. 1 shows a photo of the encapsulated source and the detector along with a schematic of the emitted X-ray beams. The X-ray intensity is recorded by the Hamamatsu C9750-10TC detector. This linear detector possesses 1280 pixels of 0.2mm with a 12bits depth. The dark image of the detector (signal with X-ray turned off) is removed from the recorded signal. The resulting signal level is proportional to the amount of X-ray received by the detector. The zero crossing linearity of the signal with variations of the exposure time has been checked. The X-ray source and detector are mounted on a rotating system so as to vary the angles of the measurements.

2.2. Void fraction measurements using X-ray attenuation

Void fraction measurements using X-ray attenuation relies on the difference of attenuation of the incident X-ray beam between the gas and liquid phases.

The attenuation of a X-ray along a material line is modelled as $dI_X = -\mu I_{X_0} dx$ which leads to Beer-Lambert law for X-ray attenuation for a given material: $I_X = I_{X_0}e^{-\mu x}$. I_{X_0} is the initial intensity of the beam, I_X is the intensity of the X-ray beam transmitted through the material, μ [in m⁻¹] is the linear attenuation of the material and x [in m] is the thickness of the material crossed by the X-ray beam. Successive attenuations through different materials lead to successive multiplications by $e^{-\mu_i x_i}$ where $\mu_i x_i$ is the attenuation coefficient of the ith material crossed. The X-ray intensity transmitted through successive elements is $I_X = I_{X_0} \prod_i e^{-\mu_i x_i}$.

In METERO experiments, the X-ray successively crosses the air, the Perspex, the flow, the Perspex and the air before reaching the X-ray detector. This is illustrated in Fig. 2. The attenuation of the X-ray beam can then be written as:

$$I_{X} = I_{X_{0}} e^{-(\mu_{air} x_{air} + \mu_{p} x_{p})} e^{-(\mu_{w} x_{w} + \mu_{b} x_{b})}$$
(1)

where $\mu_{air}x_{air}$ is the attenuation from the air outside the test section, $\mu_p x_p$ is the attenuation due to the Perspex, $\mu_w x_w$ and $\mu_b x_b$ are respectively the attenuation due to the water and the air² within the test section.

The void fraction along the X-ray path, inside the flow section, is noted α and is defined by:

$$\alpha = \frac{x_b}{x_b + x_w} = \frac{x_b}{l_{xray}}$$
(2)

 $l_{xray} = x_b + x_w$ is the length of the path of the X-ray beam within the flow.

The combination of equations (1) and (2) leads to: (I_{1})

$$\ln\left(\frac{I_X}{I_{X_0}}\right) = \underbrace{-l_{xray}(\mu_b - \mu_w)}_{A} \alpha \underbrace{-\left(\mu_{air}x_{air} + \mu_p x_p + l_{xray}\mu_w\right)}_{B}$$
$$\ln\left(\frac{I_X}{I_{X_0}}\right) = A\alpha + B \tag{3}$$

The measurement of the void fraction using X-ray attenuation relies on the determination of the constants A and B through calibration. In practice, A and B are estimated using measurements with the pipe full of air and water.³

Fig. 3a illustrates the temporal average of the signals obtained for the pipe full of air, full of water and for a slug flow. This permits to measure the void fraction along the path of the X-ray beam during each exposition of the detector. For this slug flow, Fig. 3b gives a pictorial illustration of such temporal measurements during 2.816s. Each column of the picture represents one measure of the 1D X-ray sensor and the picture is made of 1280 columns.



² subscript b for bubbles

³ This linear relation between α and $\ln(I_x/I_0)$ supposes that the effects of the hardening of the X-ray beams spectrum are negligible. The validity of this hypothesis is confirmed later.



Figure 3: (a) average recorded signal for the pipe full of air, the pipe full of water and a slug flow. The abscissa is the dimensionless projection of the pipe on the detector, noted p^* . (b) Illustration of temporal void fraction measurements (the color scale shows α) for a slug flow and a duration of 2.816s. The columns of the picture correspond to 1280 consecutive 1D measurements. For (a) and (b) the X-ray sensor is vertical, which corresponds to the position referred as 0° .



Figure 4: void fraction measurements for different water levels within the pipe. (a) void fraction measured, noted α , versus the projection of the pipe on the detector in abscissa, noted p*. The legend indicates the water level in mm. The black dots correspond to theoretical estimations on a simplified geometry. (b) Measured void fraction, α_{meas} , versus theoretical void fraction, α_{theo} , along the median vertical axis of the pipe.

The accuracy of void fraction measurements is checked by varying the water depth within the pipe while the flow is at rest. The measured void fraction can then be estimated from simplified geometrical consideration based on the level of the free surface.

Fig. 4a illustrates the comparison between measured and theoretical void fraction. The average of the root mean square of the differences between measured and theoretical values is about 0.013. This result indicates the accuracy of the void fraction measurements performed.

Fig. 4b gives the measured void fraction versus the theoretical values along the median vertical axis of the pipe. There is a good agreement between these values which follows the straight line $\alpha_{meas} = \alpha_{theo}$.

Moreover, the linearity of this result shows that the relation between $\ln(I_x/I_0)$ and α can well be considered as linear with negligible effects of the hardening of the X-ray beams spectrum in these experiments. This is thanks to the increase in voltage, i.e. X-ray energy, since previous works at 40kV [16] demonstrated such a hardening effect.

To build the vertical distribution of the void fraction within the pipe, several angular positions of the source-detector pair are needed. Indeed, the void fraction is measured along the path of the X-ray beams and these beams are not all parallel to the horizontal. To ensure deviations from the horizontal smaller than 0.5mm, between the two extremities of the flow cross section along the X-ray path, seven angular positions are needed. These positions are -3.5° , -2.25° , -1.1° , 0° , 1.1° , 2.25° and 3.5° . The vertical distribution of the void fraction is then built from these seven measurements by selecting the results minimalizing the deviation from the horizontal. It can be indicated that, with this set of angles, the mean deviation from horizontal is 0.24mm with a standard deviation of 0.14mm. This discretisation over seven angles sounds sufficient as it is about the pixel resolution of the detector and it is smaller than the targeted 0.01D resolution of the measurement.

2.3. Experimental investigations

Experimental investigations are conducted at different axial positions downstream the grid (10.4D, 20.6D and 41.3D) and for different air and water flow rates. Experiments are performed at $18.05^{\circ}C^{4}$ and atmospheric pressure.

METERO's flow map according to the liquid and gas superficial velocities, respectively $J_L = Q_{wat}/S$ and $J_G = Q_{air}/S$ where S is the flow cross section, has been established in [8] at about 40D downstream the grid. Fig. 5 gives the distribution of investigated flow parameters according to METERO's flow map (at 40D) while table 1 gives corresponding numerical values. Re_L refers to the liquid Reynolds number, $Re_L = J_L D/\nu$ where v is the kinematic viscosity of the liquid.

Water												
Q _{wat} [m3/h]	20	30	60	90	120	150						
Re_L	71 000 110 000 210 000 320 000 420 000 530 000											
$J_{L}[m/s]$	0.71	1.06	2.12	3.18	4.24	5.31						
Air												
Q _{air} [Nl/min]	10	20	30	40	50	70	90	120	150	200	250	300
$J_{G}[m/s]$	0.023	0.045	0.068	0.091	0.11	0.16	0.20	0.27	0.34	0.45	0.57	0.68

Table 1: flow parameters varied in the experiments. Nl/min corresponds to the conversion of the measured mass flow rate in l/min for 0°C and 1atm.

⁴ The variance of the recorded temperature is 0.76°C.



Figure 5: distribution of the experimental data according to METERO's flow map [8] at 40D.

3. Results and discussion

To help comparing different flow cases an inlet void fraction⁵, noted α_0 , is built as:

$$\alpha_Q = \frac{Q_{air}}{Q_{air} + Q_{wat}} \tag{4}$$

3.1. Vertical distribution of the horizontal void fraction at 41.3D

First the profile of vertical distributions of the void fraction, α , varying Q_{air} for the Reynolds number 420 000 and 110 000 are given in Fig. 6 at 41.3D.

For Re_L=420 000, the flows change from the bubble to the plug flow regime when increasing the air flow rate.⁶ For all cases, the air accumulates in the upper part of the pipe. When increasing the air flow rate, the maxima of the void fraction increase toward a maximum value of about 0.8. For the bubble flows the increase of the values of α is significantly larger than the increase in α_Q . For the plug flows the maximal value of α varies slightly and the main effect is an increase in the size of the plug and of the domain where the void fraction is significant, i.e. $\alpha \ge 0.02$.

For Re_L=110 000, the flow stays in the slug flow regime when increasing the air flow rate. The increasing of α_Q leads to an increase of the maxima of α and an increase of the domain where the void fraction is significant. The appearance of plateaus of increasing length for the maximal values is also an indication of the increase of the height of the slugs within the pipe.

Second, the profile of vertical distributions of the void fraction, α , varying Q_{wat} for the J_G values of 0.068 and 0.68 are given in Fig. 7 at 41.3D.

For $J_G=0.68$ the flows change from slug to plug and bubble flow regimes when increasing the water flow rate. As previously discussed, the slug flows cases present a plateau with an increase of the maxima values and of the domain of significant void fraction with the increase of α_Q . Two new points are interesting to note: i) the transition from slug flow to plug flow leads to an increase of the maximum value of α combined with the disappearance of the plateau; ii) the transition from plug to bubble flow regimes leads to a sharpening of the profile close to the maxima values of α and an increase of the domain where

 $^{^{5}}$ Void fraction within the plane of injection of air, i.e. at the exit of the nozzles.

⁶ The case $\alpha_Q=0.14$ correspond to a plug flow. The case $\alpha_Q=0.074$ is at the transition between plug flow and bubble flow. The cases $\alpha_Q=0.036$ and $\alpha_Q=0.016$ correspond to bubble flows.

the void fraction is significant. This can be related to the dispersion of bubbles within the core of the flow by the turbulence [8].

For $J_G=0.068$ the flows also change from slug to plug and bubble flow regimes when increasing the water flow rate. This case complements the case $J_G=0.68$ by focusing on cases with low values of α_Q . It can be noted that the bubble flow (which also corresponds to the highest Reynolds number) presents values of α larger than the other flow regimes in the core part of the flow, in particular for $0 \le y^* < 0.3$.



Figure 6: vertical distribution of the void fraction α versus y^* for J_G values of 0.68, 0.34, 0.16 and 0.068 m/s for (a) Re_L 420 000 and (b) Re_L 110 000. The corresponding values of α_Q (0.14, 0.074, 0.036, 0.016 and 0.39, 0.24, 0.13, 0.06) are indicated in the symbols' legend. x=41.3D.



Figure 7: vertical distribution of the void fraction α versus y^* for J_L values of 0.71, 2.12, 3.18 and 5.31 m/s for (a) J_G=0.68 and (b) J_G=0.068. The corresponding values of α_Q (0.49, 0.24, 0.18, 0.11 and 0.09, 0.031, 0.021, 0.013) are indicated in the symbols' legend. x=41.3D.

3.2. Changes of α distribution with the development of the flow

3.2.1. Bubble flows

Fig. 8 shows the changes in the distribution of the void fraction with the longitudinal development of two bubble flows with α_0 close to 0.116. With the longitudinal development of the flow, the void fraction

increases in the upper part of the pipe while it decreases in the bottom part for both cases. It is interesting to note that the results obtained for $J_L=4.24$ m/s and 5.31m/s looks similar for 41.3D and 20.6D respectively.

Fig. 9a directly compares these two cases while Fig. 9b compares the same cases at positions 20.6D and 10.4D. These results are relatively close. This may support that the temporal integration of buoyancy effects has evolved similarly for both cases. Fig. 9c shows the comparison between J_L =4.24m/s and 3.18m/s for α_0 about 0.021 at positions 10.4D and 41.3D. Again the two results are close.

It is important to note that the time scales during which the buoyancy effects are integrated are significantly different with ratios about 1.6 for Fig. 9a and Fig. 9b and about 3 for Fig. 9c. This highlights the importance of nonlinear processes in the development of turbulent multiphase flows.



Figure 8: α versus y^* at positions 10.4D, 20.6D and 41.3D for α_Q about 0.116. J_L values are 5.31m/s (a) and 4.24m/s (b) which respectively correspond to Re_L numbers of 530 000 and 420 000.



Figure 9: vertical distribution of the void fraction α versus y^* ; (a,b) α_Q about 0.116 (a) J_L =4.24m/s at 20.6D and J_L =5.31 m/s at 41.3D, (b) J_L =4.24m/s at 10.4D and J_L =5.31 m/s at 20.6D; (c) α_Q =0.021 J_L =4.24m/s at 41.3D and J_L =3.18 m/s at 10.4D.

3.2.2. Slug flows and complex transitions

Fig. 10 shows the evolution of the profile of α versus y^* at positions 10.4D, 20.6D and 41.3D for $\alpha_Q=0.113$, $J_L=2.12$ m/s and $J_L=0.71$ m/s. It can be noted that as opposed to the bubble flows cases, the void fraction maxima decreases with the longitudinal development of the flow. Two different reasons can be highlighted: i) in the case of Fig. 10a the flow regime changes from position 10.4D to 41.3D. At 10.4D the flow looks like a bubble flow with a continuous plug (or foam) at the top. At 41.3D the flow has

evolved toward a slug flow; ii) The flow regime is similar to a slug flow for the three positions. What is observed is an increase of the height of the slugs with a decrease of their frequency.



Figure 10: α versus y^* at positions 10.4D, 20.6D and 41.3D for α_Q about 0.113. J_L values are 2.12m/s (a) and 0.71m/s (b) which respectively correspond to Re_L numbers of 210 000 and 71 000

3.3. Void fraction in the flow cross-section versus α_Q and relative phase velocities

The void fraction in the flow cross-section is estimated by integrating the horizontal void fraction over y^* :

$$\alpha_S = \frac{1}{S} \int_{-0.5}^{0.5} \alpha l_{y^*} D dy^*$$
(5)

where S is the area of the flow cross-section, l_{y^*} is the horizontal chord length at the height y^* .

Fig. 11a gives α_S versus α_Q at 41.3D. It can be noted that α_S is closer to α_Q for bubble flows than for slug flows. Moreover, it is observed that for bubble flows $\alpha_S \sim \alpha_Q$ and that for slug flows $\alpha_S \sim \frac{3}{\pi} \alpha_Q$.

The average cross section of air and water can be calculated using α_s . The mean air and water velocities, i.e. phase velocities of air and water, respectively noted U_{air} and U_{wat} can then be estimated as:

$$U_{air} = \frac{Q_{air}}{\alpha_S S} = \frac{J_G}{\alpha_S} \tag{6}$$

$$U_{wat} = \frac{Q_{wat}}{(1 - \alpha_S)S} = \frac{J_L}{1 - \alpha_S} \tag{7}$$

From the measure of U_{air}/U_{wat} at 41.3D, it can be shown that the slugs of air are generally moving faster than the water. Fig. 11b shows U_{air}/U_{wat} versus α_Q at position 41.3D.

For the slug flows, the variations of U_{air}/U_{wat} are observed to vary like $\frac{5}{2}\alpha_Q$.

For the bubble flows, the mean speed of air is observed to be smaller than the mean speed of water. This is due to the accumulation of air in the upper part of the flow where the increase of friction leads to a local decrease of the flow speed whilst the flow speed increases in the lower part of the pipe when compared to the upper part and/or to the single-phase water flow [8]. U_{air}/U_{wat} is closer to 1 for the highest Reynolds number than for the two others. This is due to a larger turbulence dispersion of bubbles leading to a higher void fraction on (and below) the pipe axis in the case of the highest turbulent intensity.

For plug flows it is generally observed that the mean velocity of air is smaller than the mean velocity of water for similar reasons than for the bubble flow cases.



4. CONCLUSIONS

The basics of void fraction measurements using X-ray attenuation and the construction of the vertical distribution of the horizontal void fraction have been exposed before presenting results obtained from such measurements applied to multiphase flows in a horizontal pipe.

The vertical void fraction profiles are discussed accordingly to flows Reynolds numbers, injected void fraction α_Q and the development of the multiphase flows along the pipe. Positions investigated are 10.4D, 20.6D and 41.3D.⁷

The accumulation of void fraction in the upper part of the pipe is set in evidence in all cases.

The non-linearity of the evolution of the void fraction profiles with the flows travelling time is also highlighted for similar α_Q . This is attributed to the importance of non-linear coupling between the effects of buoyancy forces and turbulence over the settling of multiphase flows.

Using the integration of α over the pipe height, the void fraction within the cross section α_s is estimated for measurements obtained at 41.6D. It is observed that for bubble flows $\alpha_s \sim \alpha_q$ and that for slug flows $\alpha_s \sim \frac{3}{5} \alpha_q$.

The phase velocities are deduced from superficial velocities and α_s . It is observed that due to the accumulation of bubbles in the upper part of the flow where the flow is going slowly than in the bottom part [8] the air phase velocity is generally smaller than the water phase velocity for bubble and plug flows. On the contrary, the air phase velocity is generally higher than the water phase velocity for slug flows. In addition, it is observed that U_{air}/U_{wat} varies like $\frac{5}{2}\alpha_0$ for slug flows.

ACKNOWLEDGMENTS

Authors would like to acknowledge Muriel Marchand. This work has been achieved in the framework of the NEPTUNE project, financially supported by CEA (Commissariat à l'Energie Atomique et aux Energies Alternatives), EDF, IRSN (Institut de Radioprotection et de Sûreté Nucléaire) and AREVA-NP.

⁷ Experiments are planned to be performed at 1D so as to provide inlet conditions for numerical simulations willing to investigate the longitudinal development of turbulent multiphase flows in horizontal pipes.

REFERENCES

- S.K. Wang, S.J. Lee, O.C. Jones, and R.T. Lahey, "3-D turbulence structure and phase distribution measurements in bubbly two-phase flows," *Int. J. Multiphase Flow*, vol. 13, no. 3, pp. 327-343, 1987.
- [2] M. Lance and J. Bataille, "Turbulence in the liquid phase of a uniform bubbly air-water flow," *J. Fluid Mech.*, vol. 222, pp. 95-118, 1991.
- [3] T.J. Liu and S.G. Bankoff, "Structure of air-water bubbly flow in a vertical pipe I. Liquid mean velocity and turbulence measurements," *Int. J. Heat Mass Transfer*, vol. 36, no. 4, pp. 1049-1060, 1993.
- [4] T.J. Liu and S.G. Bankoff, "Structure of air-water bubbly flow in a vertical pipe II. Void fraction, bubble velocity and bubble size distribution," *int. J. Heat Mass Transfer*, vol. 36, no. 4, pp. 1061-1072, 1993.
- [5] C. Suzanne, K. Ellingsen, F. Risso, and V. Roig, "Local measurements in turbulent bubbly flows," *Nuclear Engineering and Design*, vol. 184, pp. 319-327, 1998.
- [6] P. Andreussi, A. Paglianti, and F. Sanchez Silva, "Dispersed bubble flow in horizontal pipes," *Chem. Eng. Sci.*, vol. 54, pp. 1101-1107, 1999.
- [7] D. Barnea, "A unified model for predicting flow-pattern transitions for the whole range of pipe inclinations," *Int. J. Multiphase Flow*, vol. 13, no. 1, pp. 1-12, 1987.
- [8] M. Bottin et al., "Experimental investigation of a developing two-phase bubbly flow in horizontal pipe," *Int. J. Multiph. Flow*, vol. 60, pp. 161-179, 2014.
- [9] H.M. Prasser, M. Misawa, and I. Tiseanu, "Comparison between wire-mesh sensor and ultra-fast X-ray tomograph for an air-water flow in a vertical pipe," *Flow Measurement and Instrumentation*, vol. 16, pp. 73-83, 2005.
- [10] V. Aeschlimann, S. Barre, and S. Legoupil, "X-ray attenuation measurements in a cavitating mixing layer for instantaneous two-dimensional void ratio determination," *Phys. Fluids*, vol. 23, p. 055101, 2011.
- [11] T.J. Heindel, "A review of X-Ray flow visualization with applications to multiphase flows," *Journal of Fluids Engineering*, vol. 133, p. 074001, 2011.
- [12] A. Kastengren and C.F. Powell, "Synchrotron X-ray techniques for fluid dynamics," *Exp. Fluids*, vol. 55, p. 1686, 2014.
- [13] R.W. Pike, B. Wilkins, and H.C. Ward, "Measurement of the Void Fraction in Two-Phase Flow by X-Ray Attenuation," A.1.Ch.E. Journal, vol. 11, no. 5, pp. 794-800, 1965.
- [14] M. Botin, "Stratification d'un écoulement diphasique horizontal: modélisation et validation expérimentale," *PhD thesis Grenoble INP*, 2010.
- [15] O.C. Ozturk, "Contribution expérimentale et numérique à l'amélioration des modèles de transition de régime en écoulement diphasique horizontal," *PhD thesis*, 2013.
- [16] Emmanuel Jouet, "Mise au point d'une technique de mesure de taux de présence local par tomographie à rayons X," Grenoble INP, Thesis 2001.